

# A BRIEF HISTORY OF OPTIMIZATION-BASED ILC. WHAT'S NEXT?

*17/03/2022 @ Syscop, University of Freiburg*

MECO  
RESEARCH TEAM

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# OUTLINE

## Introduction

### Opt-ILC: a brief history

- Filter based an Model-inversion ILC
- Norm-Optimal ILC
- Optimization based ILC
- RoFaLT

### Applications and developments

- Applications
- Multi-system ILC
- ECOset-ILC

## Conclucision

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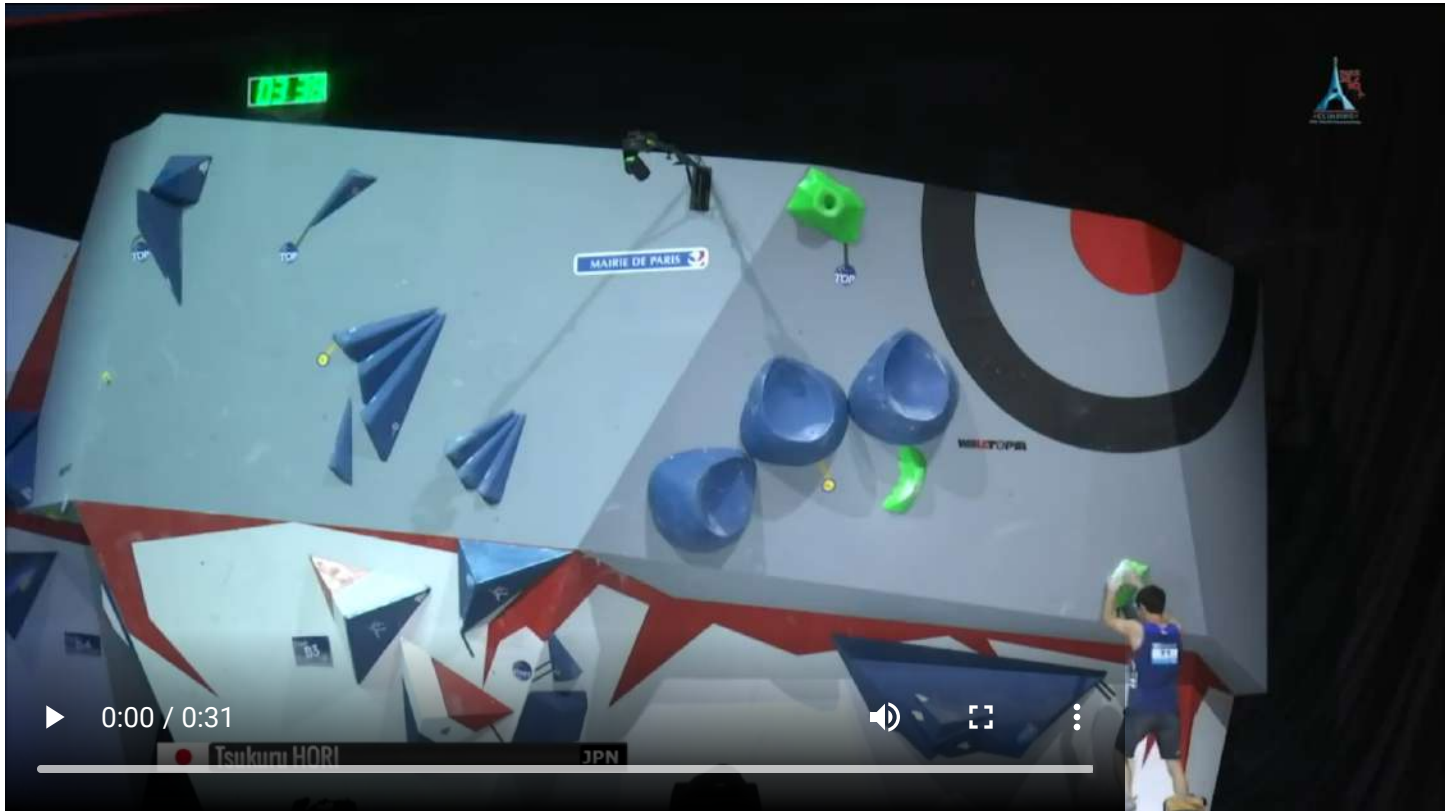
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What is ILC?



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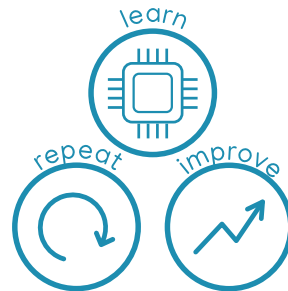
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- learn from previous trials and improve
- offline strategy
- Feed-forward/open-loop
- Plug-in to existent control system

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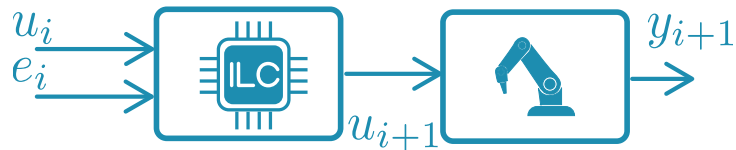
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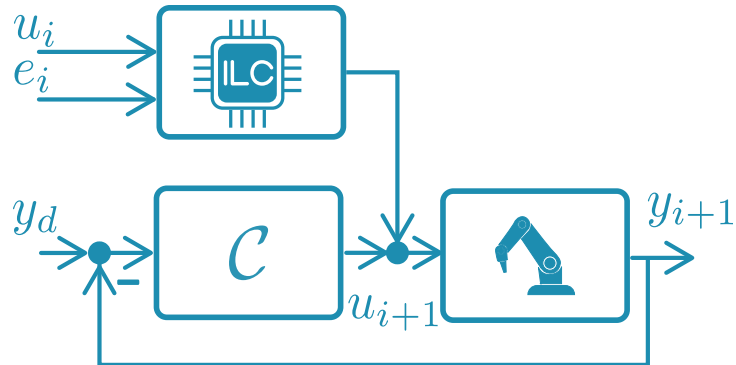




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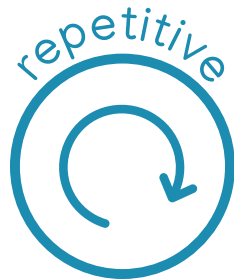
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- the task is repetitive
- same initial conditions
- compensate repetitive errors
  - model-plant mismatch
  - exogenous disturbances

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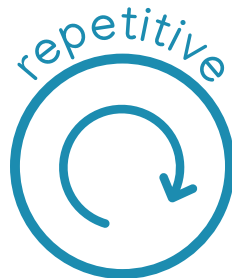
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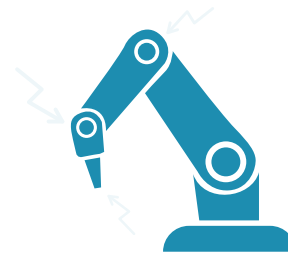
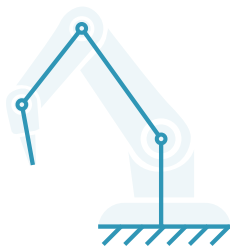
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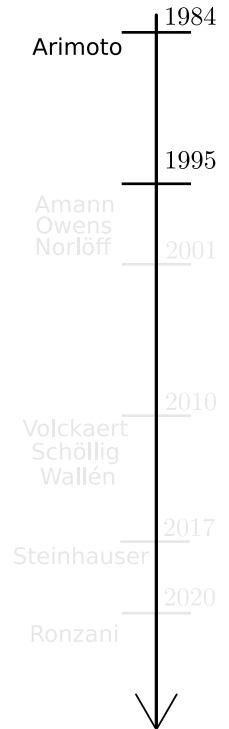
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From  $\mathcal{LQ}$ -filter to norm-optimal ILC

How to get fast convergence and high performance?



Model-inversion





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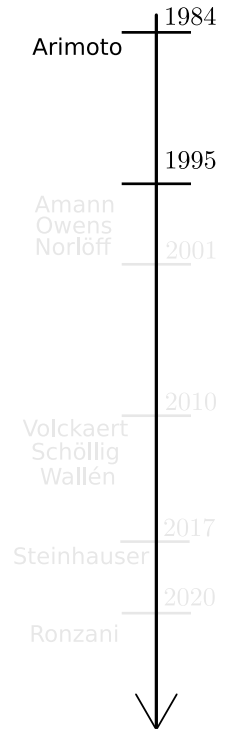
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$$e_i = y_d - y_i$$

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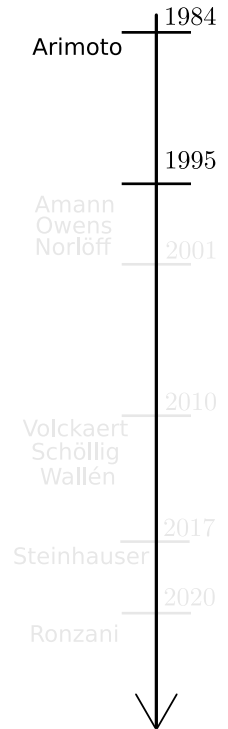
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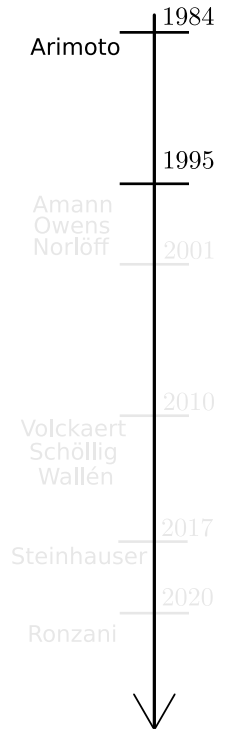
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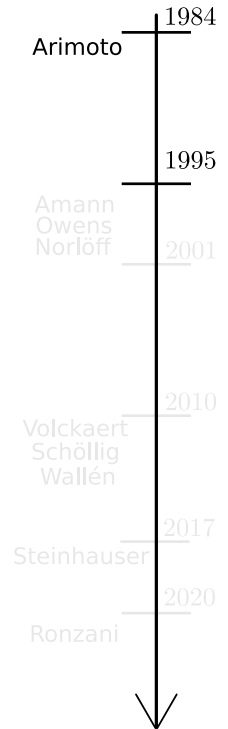
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$$y_0 = 0$$

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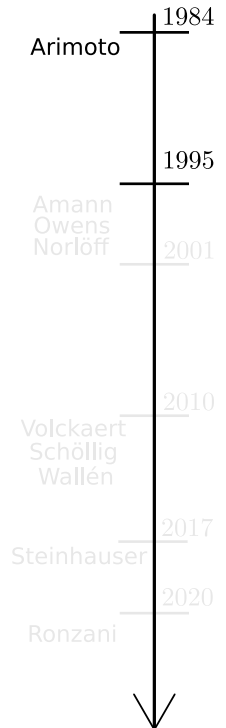
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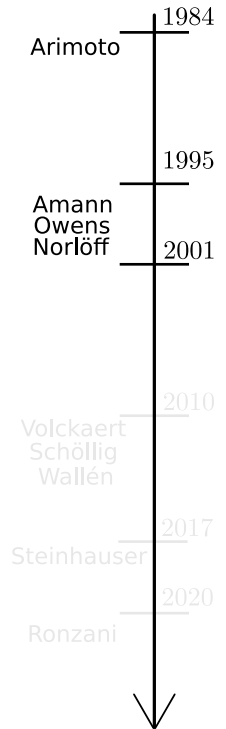
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From  $\mathcal{LQ}$ -filter to norm-optimal ILC

- Optimal control approach
- In practice:
- Equivalence in the filter design framework:

$$\mathcal{Q} = (\hat{P}^T Q \hat{P} + R_1 + R_2)^{-1} (\hat{P}^T Q \hat{P} + R_2)$$
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Can this be generalized even further?



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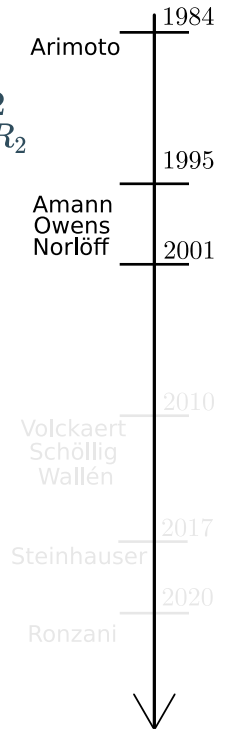
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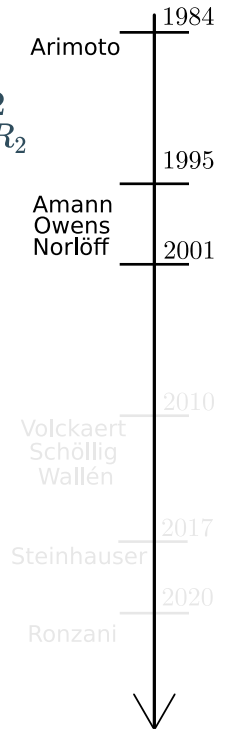
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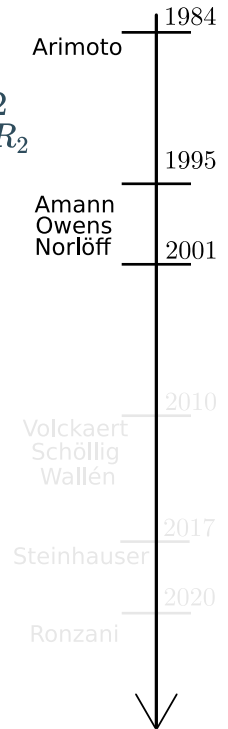
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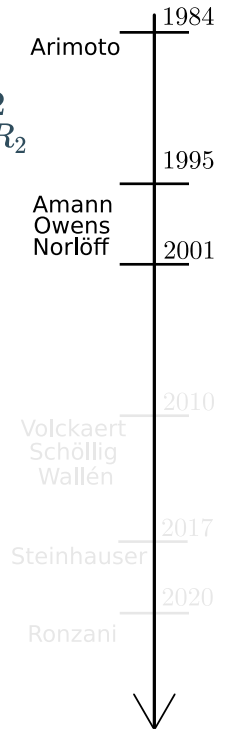
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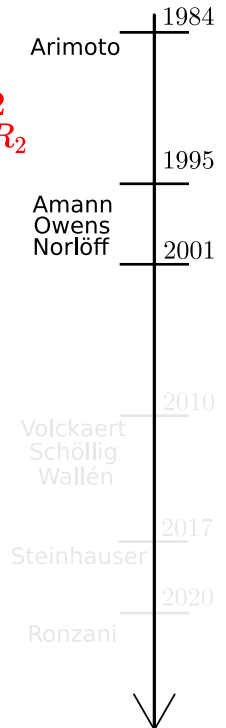
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- In practice:  $Pu \approx \hat{P}u + (y_i - \hat{P}u_i)$  **model correction**
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## Optimization-based ILC

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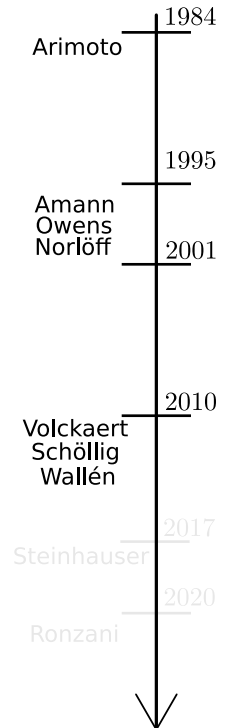
$$\beta_i = \arg \min_{\beta} \|y_i - \hat{\mathcal{P}}(u, \beta)\|_V^2 + \|\beta\|_{W_1}^2 + \|\beta - \beta_{i-1}\|_{W_2}^2$$

- Observer-based/Kalman filter estimation
- Disturbances/parameter estimation

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$$u_{i+1} = \arg \min_u \|y_d - \hat{\mathcal{P}}(u, \beta_i)\|_Q^2 + \|u\|_{R_1}^2 + \|u - u_i\|_{R_2}^2$$

- other type of tasks can be considered, e.g. time-optimal motion
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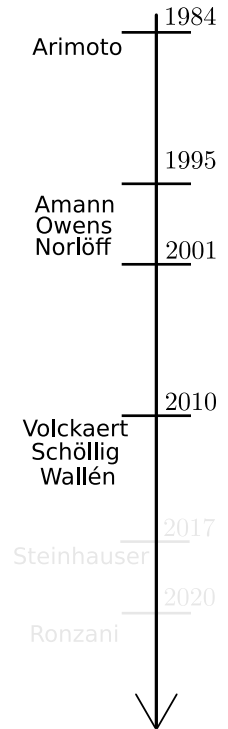
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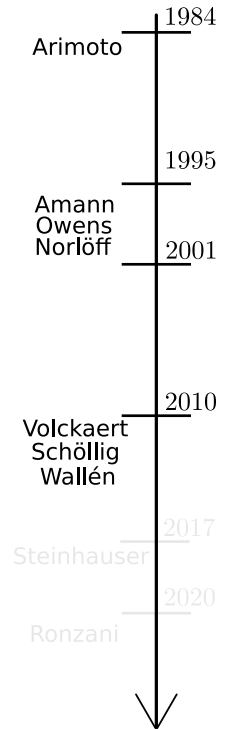
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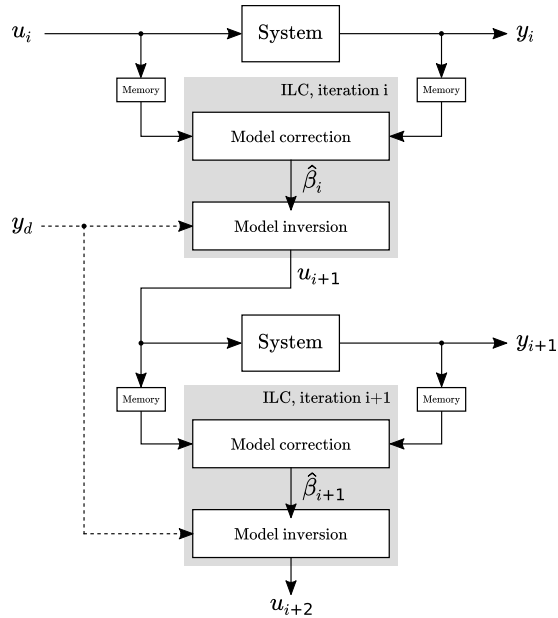
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# OPT-ILC: A BRIEF HISTORY

## RoFaLT: two-step nonlinear ILC



```

1  myRoFaLT = rofalt.RoFaLT();
2
3  doc rofalt.RoFaLT
4
5  model = myRoFaLT.setModel('ts', 0.01, ...
6                      'ode', odeFcn, ...
7                      'output', yFcn);
8
9  ilc = myRoFaLT.setController('ilc');
10
11 ilc.setReference(ref);
12
13 ilc.control.addInequalityConstraints(usym, ...
14                                 umin, umax)
15
16 for i = 1:1:nTrials
17     umeas = ilc.runIteration(struct('u', umeas, ...
18                               'y', ymeas));
19
20     ymeas = executeMeasurements(umeas);
21 end
22
23 results = ilc.getResults();
24

```

Arimoto	1984
Amann Owens Norlöff	1995 2001
Volckaert Schöllig Wallén	2010
Steinhauser	2017
Ronzani	2020



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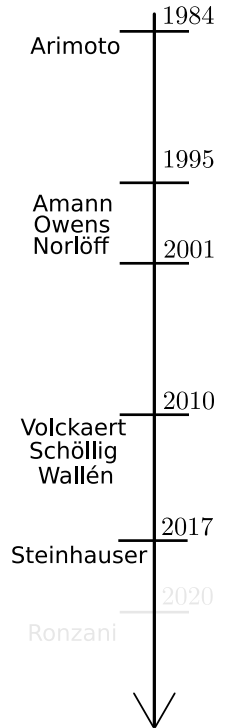
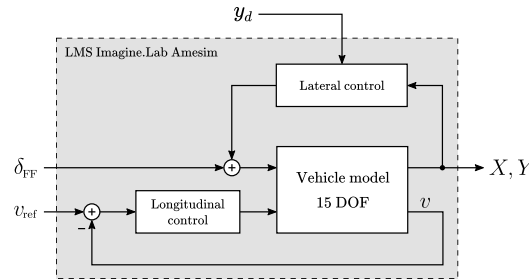
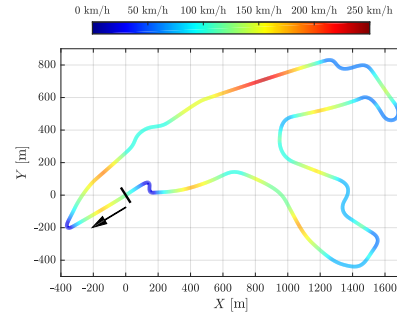
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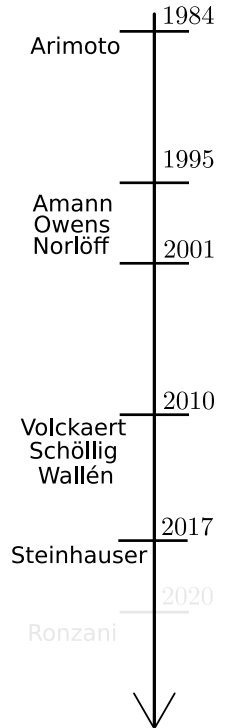
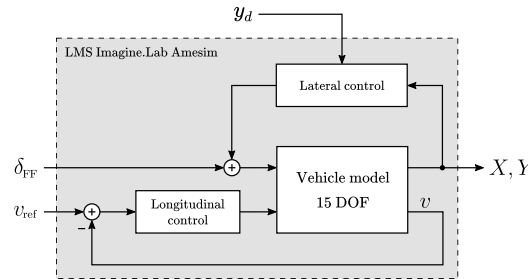
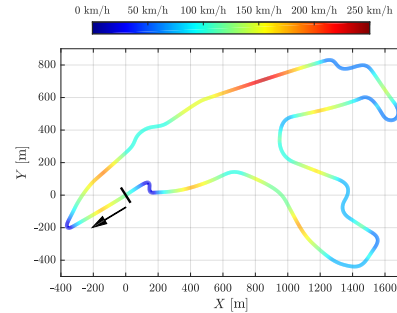
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  - Input correction
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  - Constraints: input saturation



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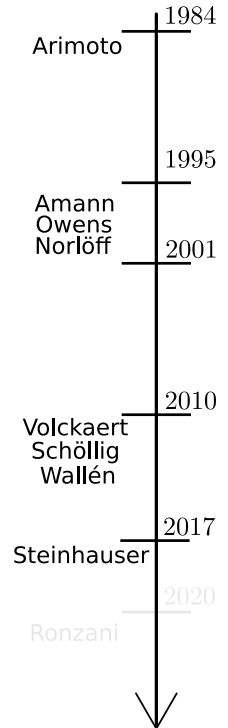
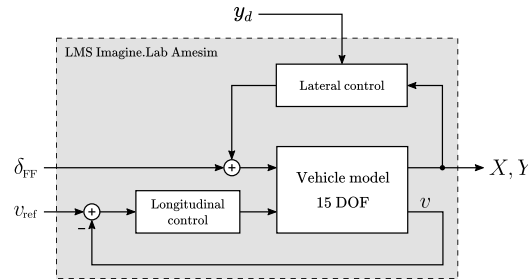
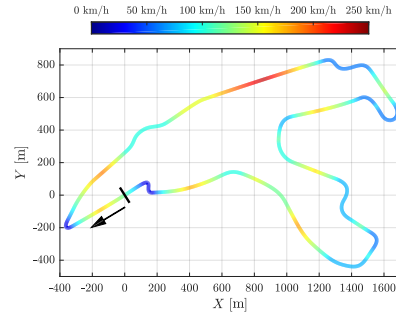
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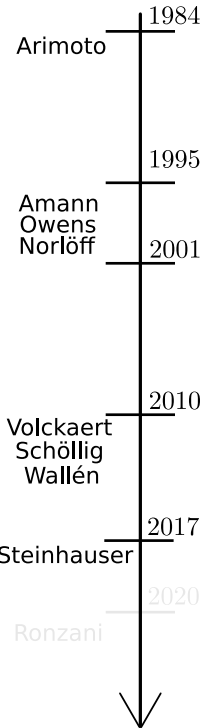
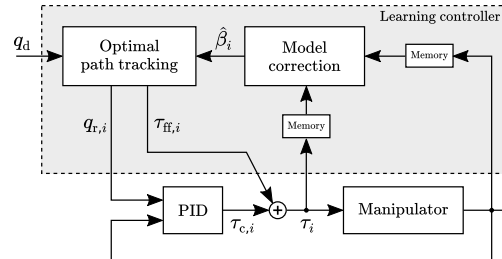
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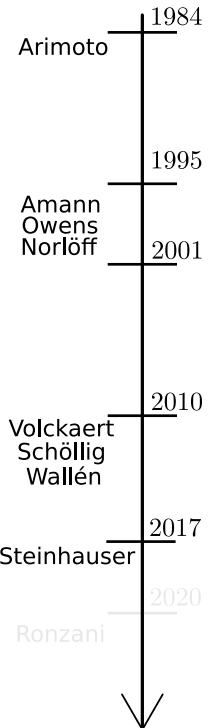
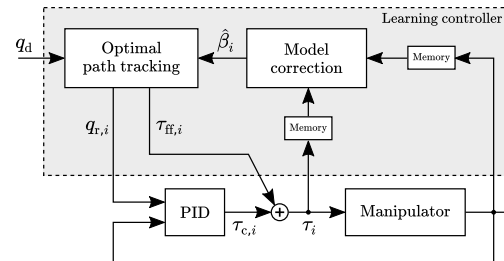
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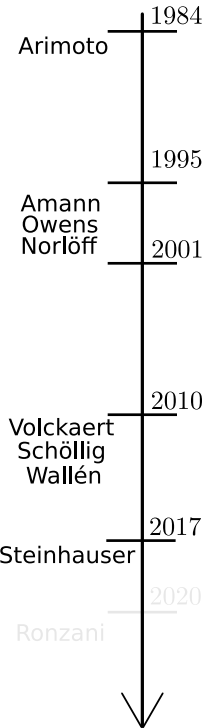
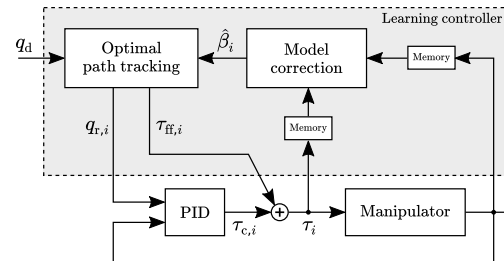
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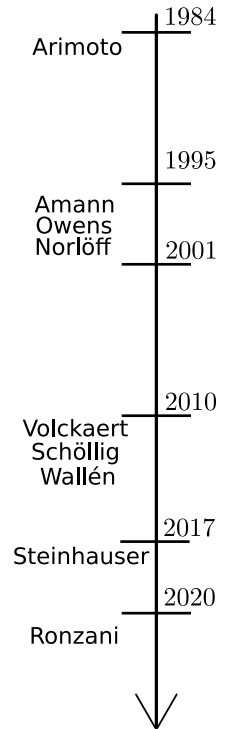
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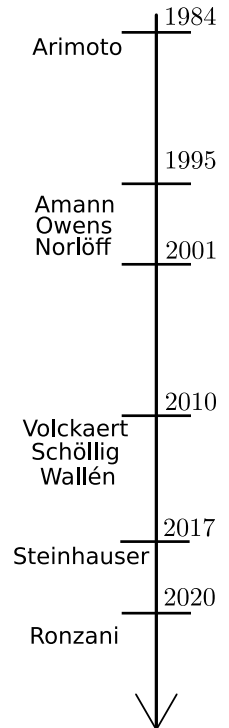
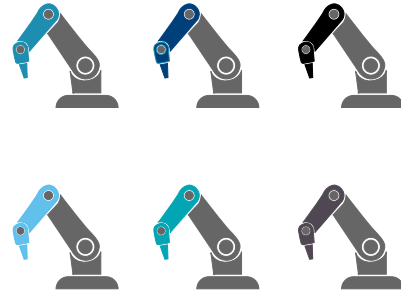
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  - Repetitive task
  - Iterative Learning Control
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- Industry 4.0: interconnected systems
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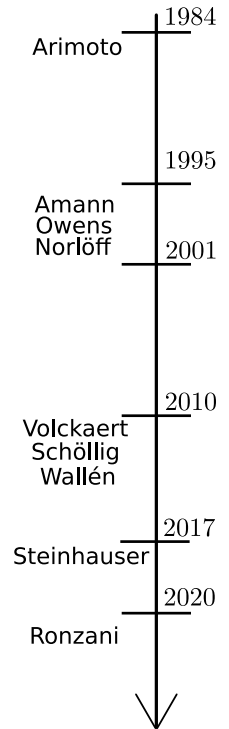
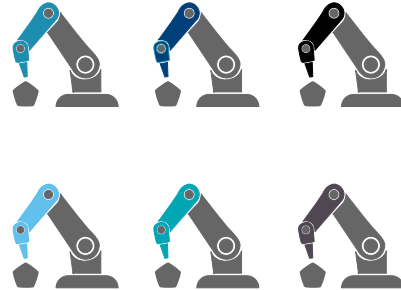
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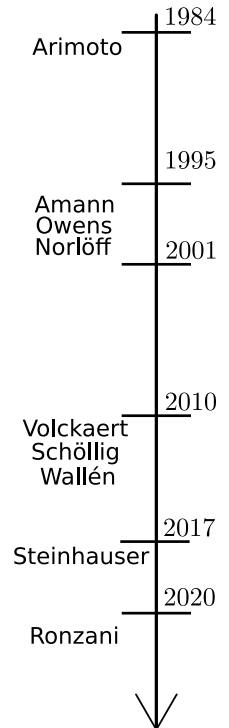
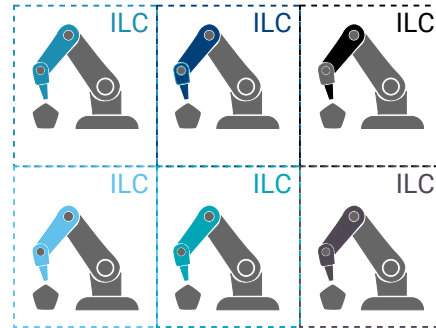
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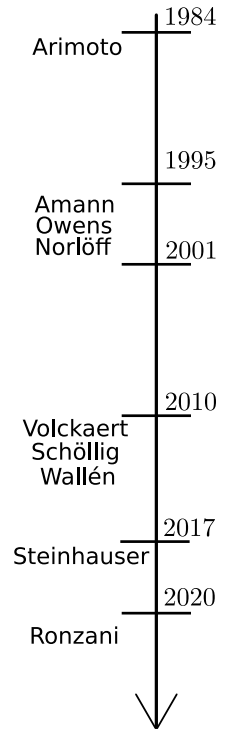
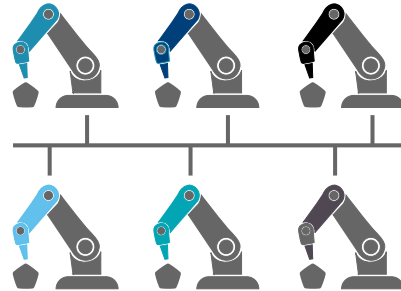
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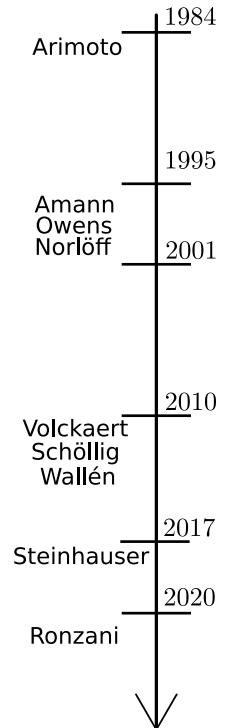
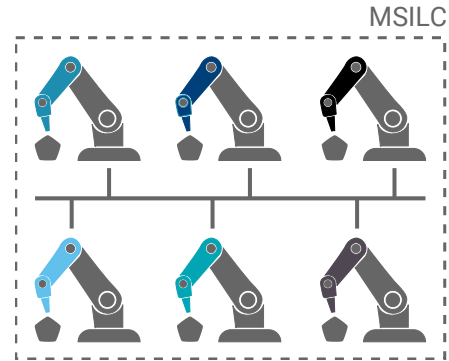
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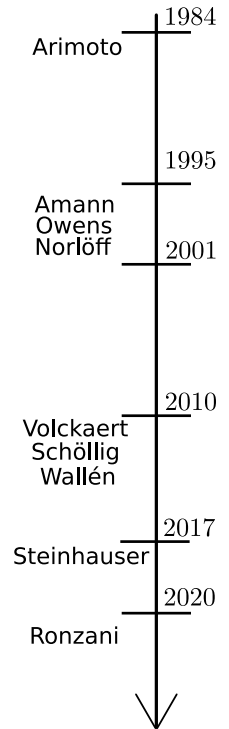
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## Multi-system ILC

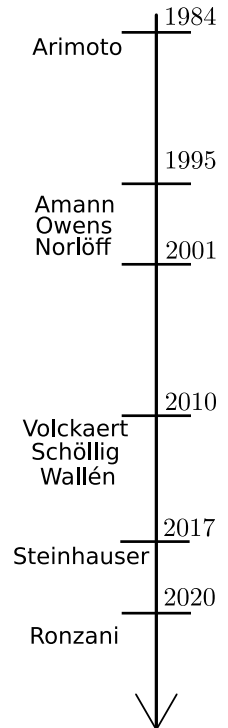
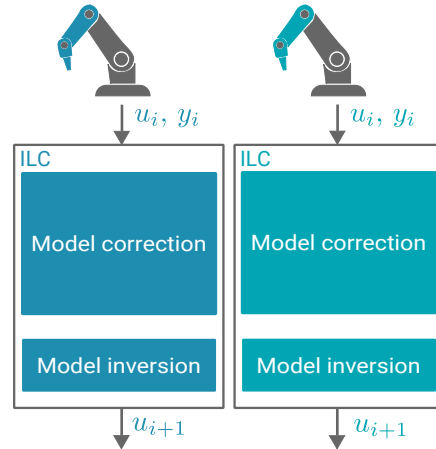
- Model correction: common+delta
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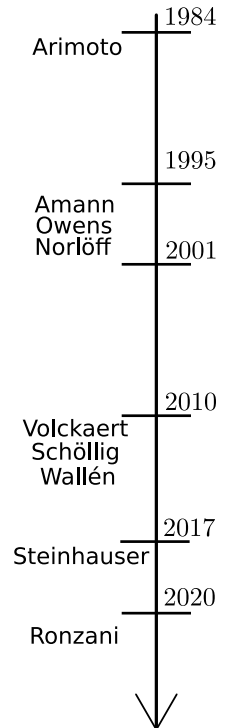
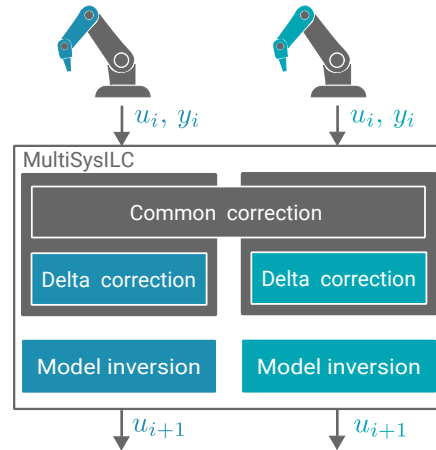




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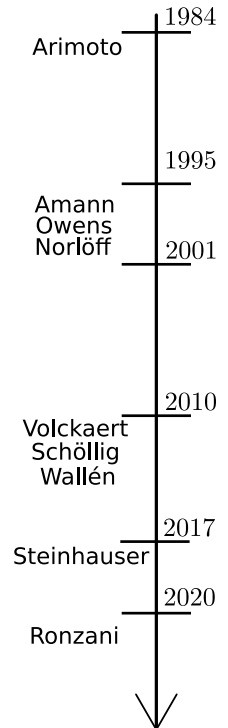
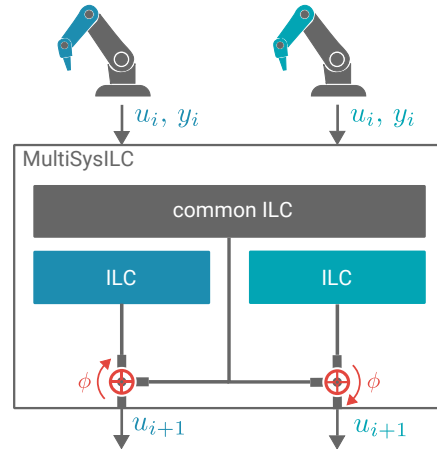
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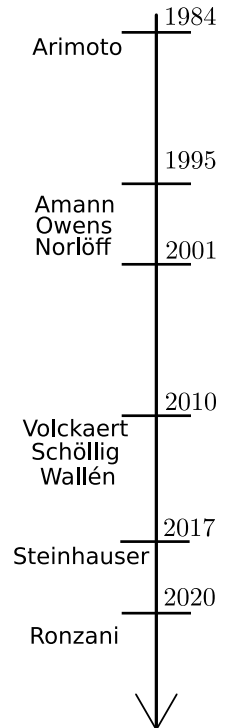
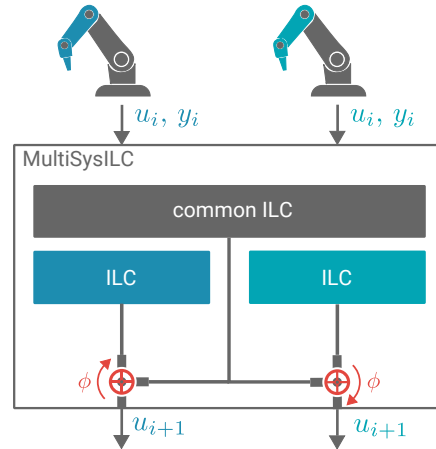
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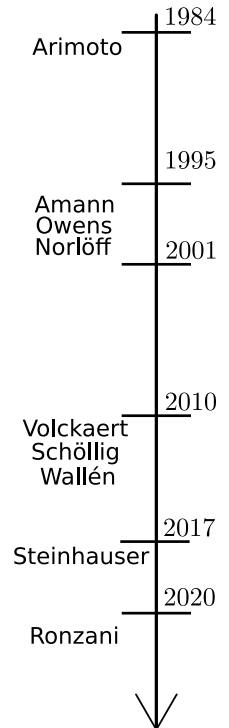
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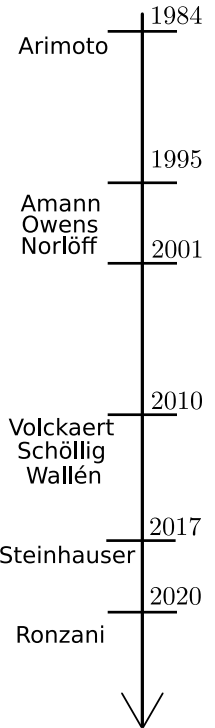
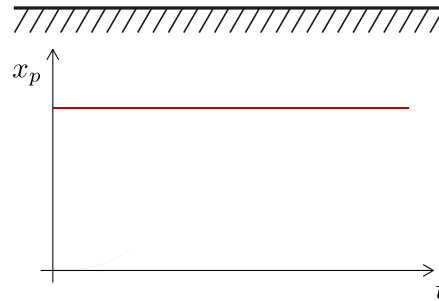
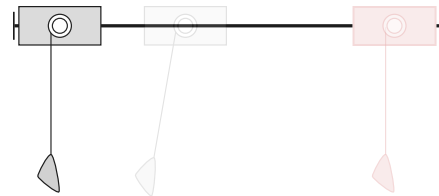
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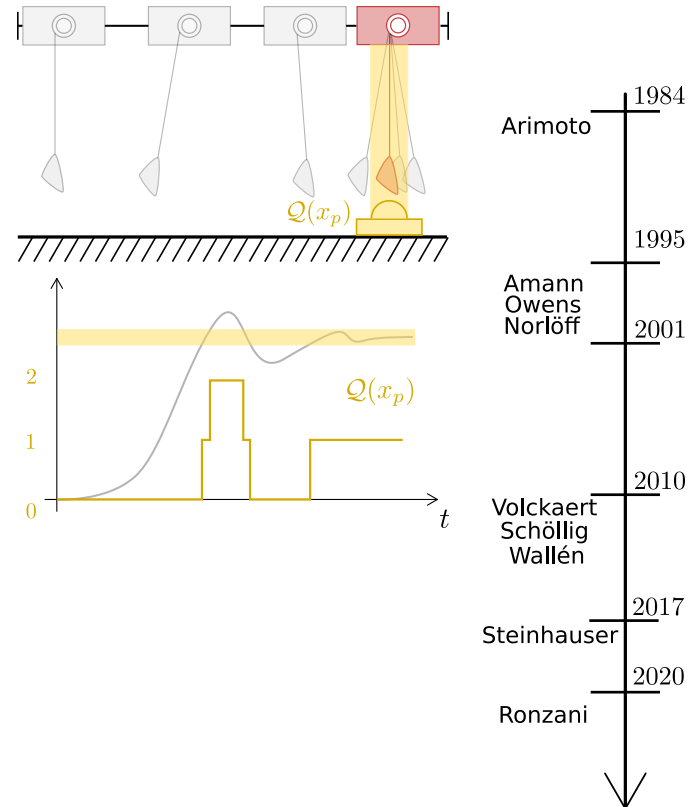
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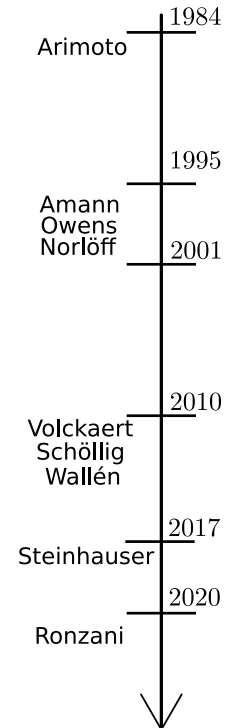
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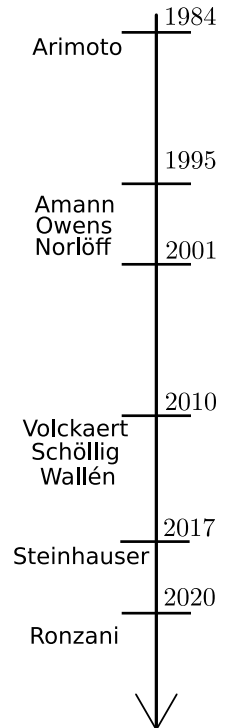
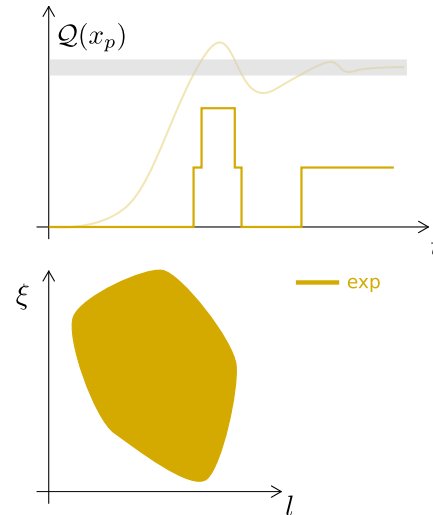
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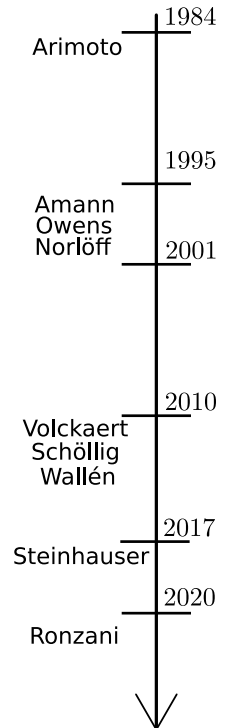
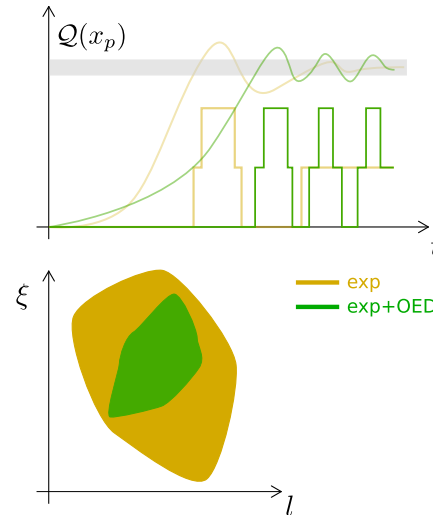




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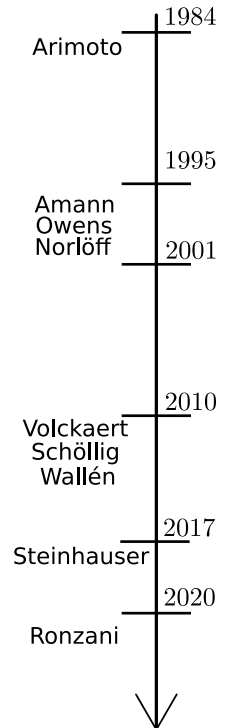
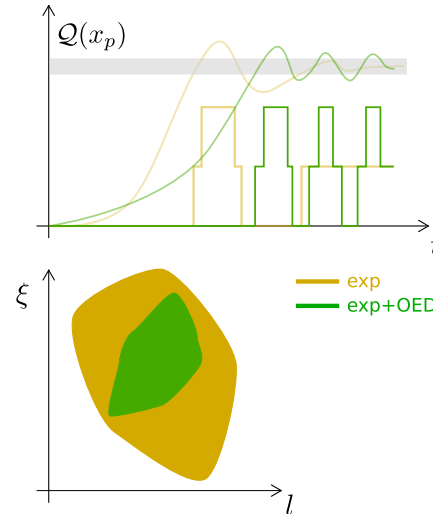
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# NEXT?

## Task flexibility in ILC

- Model
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  - non-parametric corrections:  $\beta$  represents a disturbance
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Stability and convergence analysis

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- Model correction: additive disturbance (no optimization problem)
- Model inversion: Tracking error minimization
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$\mathcal{LQ}$  framework analysis



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Stability and convergence analysis

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ZOO-ILC (Baumgärtner, Diehl 2020)

# CONCLUSION

Stability and convergence analysis

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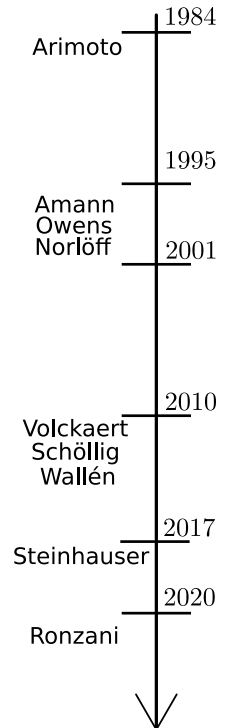


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# REFERENCES

## A brief history of pptimization-based ILC

1. S. Arimoto, S. Kawamura, and F. Miyazaki, "Bettering operation of Robots by learning: A new control theory for servomechanism or mechatronics systems," J. Robot. Syst., 1984.
2. N. Amann, D. H. Owens, and E. Rogers, "Iterative learning control for discrete-time systems with exponential rate of convergence," IEE Proc. Control Theory Appl., vol. 143, no. 2, pp. 217–224, 1996.
3. S. Gunnarsson and M. Norrlöf, "On the design of ILC algorithms using optimization," Automatica, vol. 37, no. 12, pp. 2011–2016, Dec. 2001.
4. A. P. Schoellig and R. D'Andrea, "Optimization-based iterative learning control for trajectory tracking," in 2009 European Control Conference, ECC 2009, 2009, pp. 1505–1510.
5. M. Volckaert, J. Swevers, and M. Diehl, "A Two Step Optimization Based Iterative Learning Control Algorithm," ASME 2010 Dyn. Syst. Control Conf. Vol. 1, pp. 579–581, Jan. 2010.
6. J. Wallén, M. Norrlöf, and S. Gunnarsson, "A framework for analysis of observer-based ILC," Asian J. Control, vol. 13, no. 1, pp. 3–14, Jan. 2011.
7. S. Gunnarsson and M. Norrlöf, "On the design of ILC algorithms using optimization," Automatica, vol. 37, no. 12, pp. 2011–2016, Dec. 2001.
8. A. Steinhauser, T. D. Son, E. Hostens, and J. Swevers, "RoFaLT : An Optimization-based Learning Control Tool for Nonlinear Systems," 2018 IEEE 15th Int. Work. Adv. Motion Control, pp. 198–203, Mar. 2018.
9. A. Steinhauser and J. Swevers, "An efficient iterative learning approach to time-optimal path tracking for industrial robots," IEEE Trans. Ind. Informatics, vol. 14, no. 11, pp. 5200–5207, Nov. 2018.
10. D. Ronzani, A. Steinhauser, and J. Swevers, "Multi-System Iterative Learning Control: an Extension of ILC for Interconnected Systems," in 2020 IEEE 16th International Workshop on Advanced Motion Control (AMC), 2020, pp. 79–84.
11. K. Baumgartner and M. Diehl, "Zero-Order Optimization-Based Iterative Learning Control," in Proceedings of the IEEE Conference on Decision and Control, 2020, vol. 2020-Decem, pp. 3751–3757.
12. D. Ronzani, J. Gillis, G. Pipeleers, and J. Swevers, "EC0set-ILC: an Iterative Learning Control Approach with Set-membership Uncertainty," 2022 IEEE 17th Int. Conf. Adv. Motion Control, pp. 68–75, Feb. 2022.



Thank you for your attention.

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