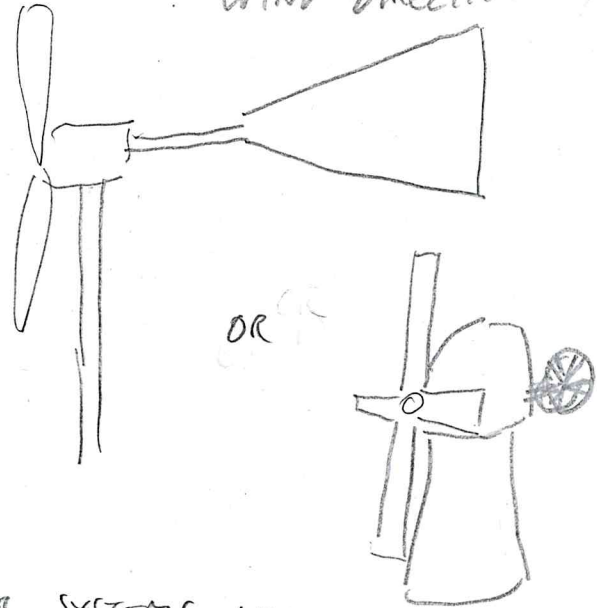


# CHAPTER 5: CONTROL OF WIND TURBINES

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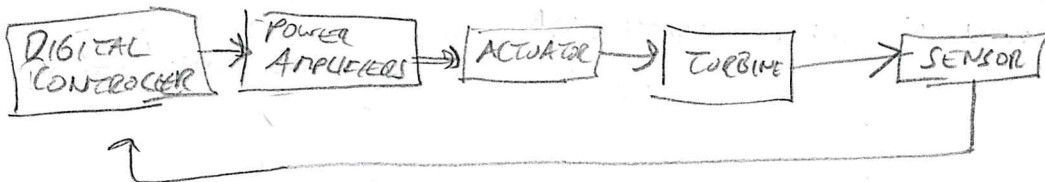
SOMETIMES:

- a) PASSIVE CONTROL BY MECHANICAL DESIGN, EG. VANE OR TAIL-ROTTES TO ORIENT TURBINE INTO WIND DIRECTION



MOSTLY:

- b) ACTIVE CONTROL BY SENSOR-ACTUATOR SYSTEMS, USUALLY USING DIGITAL CONTROLLERS



## 5.1 SENSORS & ACTUATORS IN WIND TURBINES

### SENSORS

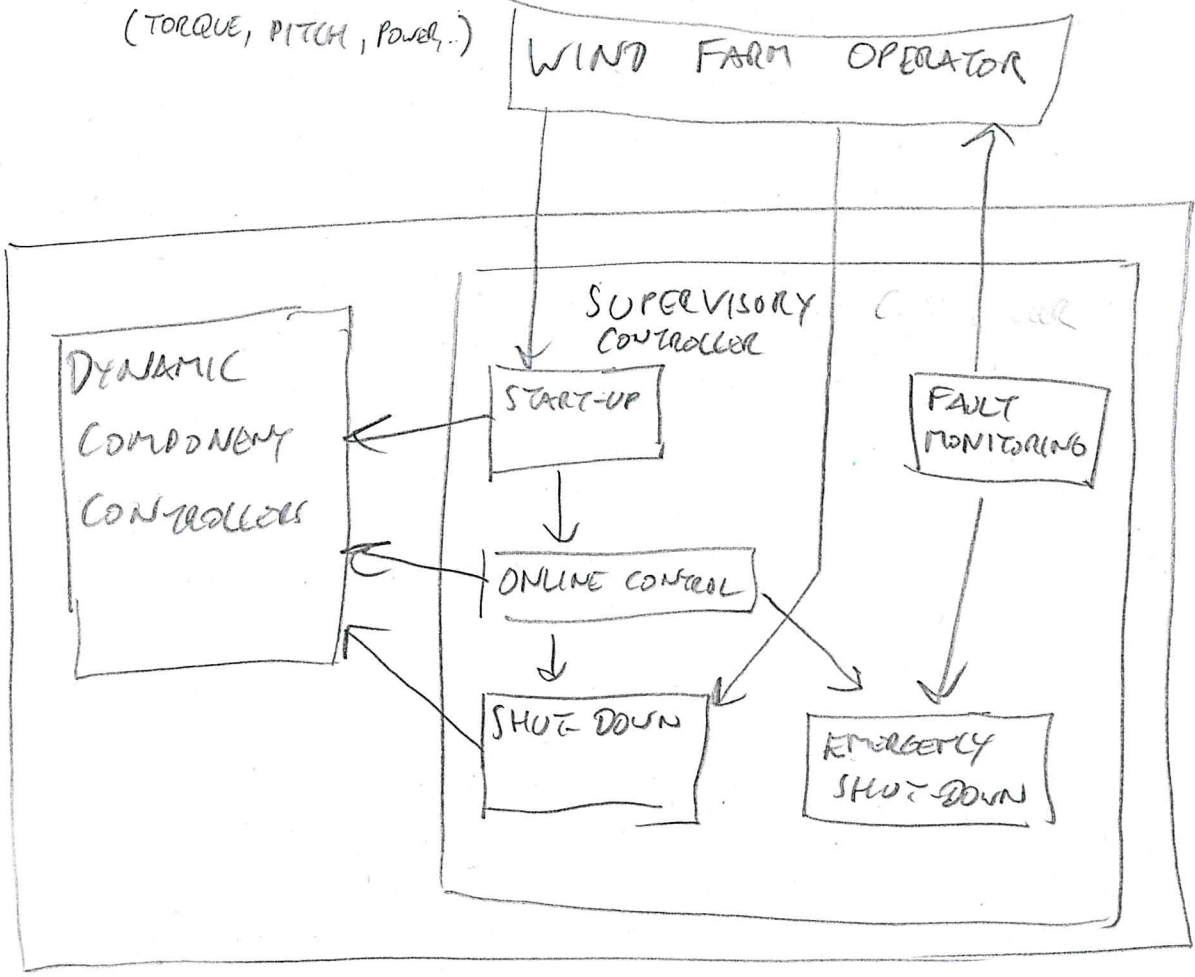
- GENERATOR SPEED, ROTOR SPEED, WIND SPEED, YAW RATE
- TEMPERATURES (GEARBOX OIL, GENERATOR WINDING, AMBIENT AIR, ...)
- BLADE PITCH, BLADE AZIMUTH, YAW ANGLE, WIND DIRECTION
- GRID POWER, CURRENT, VOLTAGE, GRID FREQUENCY, ...)
- TOWER TOP ACCELERATION, GEARBOX VIBRATION, SHAFT TORQUE, BLADE ROOT BENDING MOMENT
- ENVIRONMENT: ICING, HUMIDITY, LIGHTNING

ACTUATORS:

- GENERATOR
- MOTORS: PITCH, YAW,
- LINEAR MOTORS, MAGNETS, SOLID STATE SWITCHES
- HYDRAULIC PUMPS & PISTONS (HIGH POWER & SPEED)
- RESISTANCE HEATERS & FANS FOR TEMPERATURE CONTROL
- BRAKES (ROTOR, YAW)

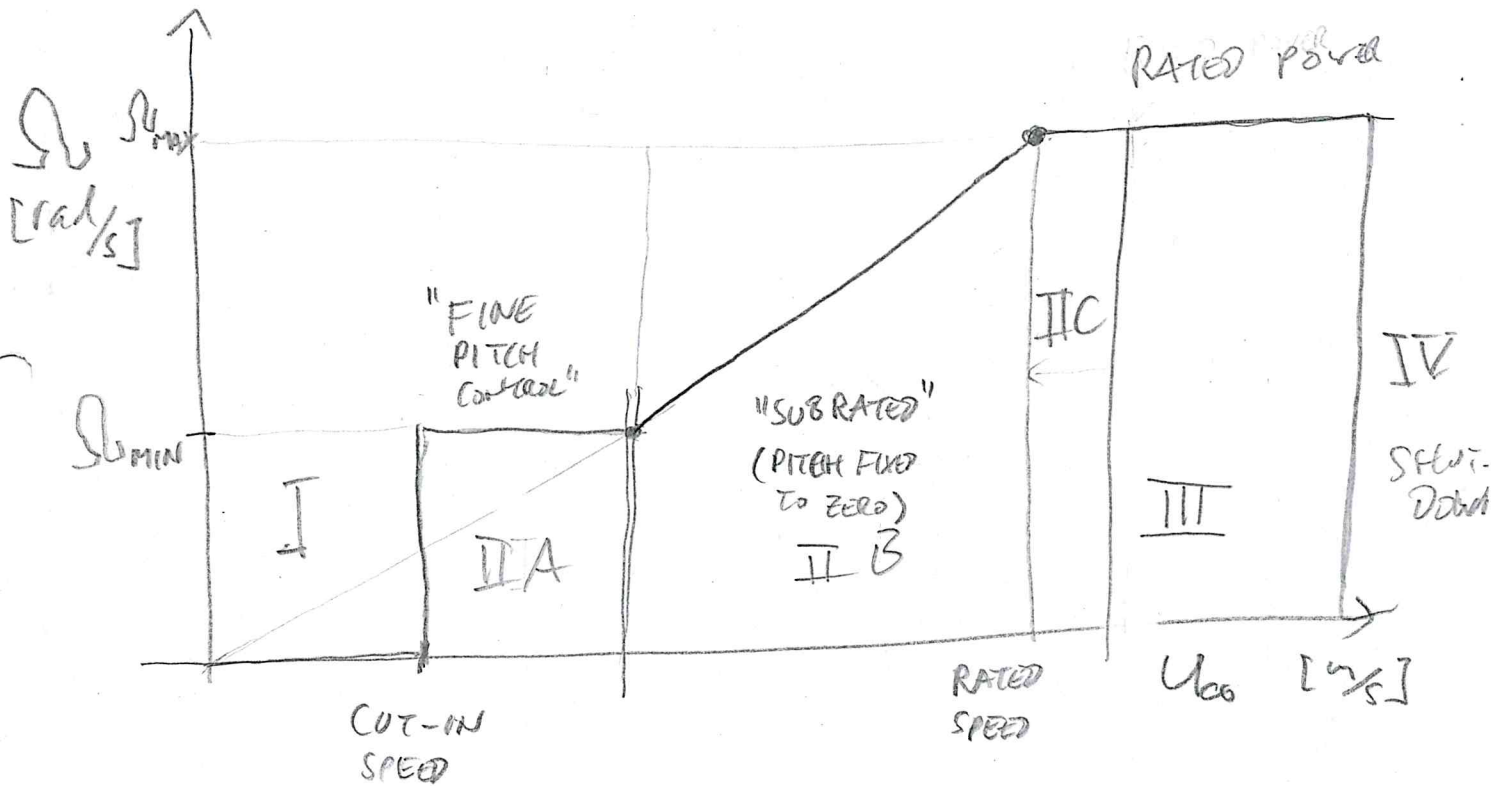
5.2 CONTROL SYSTEM ARCHITECTURE

USUALLY, "SUPERVISORY CONTROL" ON HIGH LEVEL FOR (FIXTURE) TURBINE OPERATIONS STATES, AND "DYNAMIC CONTROL" ON LOWER LEVEL (TORQUE, PITCH, POWER...)



# 5.3 CONTROL OF VARIABLE SPEED TURBINES

ROTATION SPEED AS FUNCTION OF WIND SPEED,  
FOR VARIABLE SPEED, PITCH CONTROLLED TURBINE



AIM: MAXIMUM POWER PRODUCTION / COEFFICIENT  $C_p(\lambda, \beta)$

PROBLEM: WIND SPEED ON ROTOR DISC NOT PERFECTLY KNOWN

POWER: 
$$P = \frac{1}{2} \rho A U_{\infty}^3 \cdot C_p(\lambda, \beta)$$

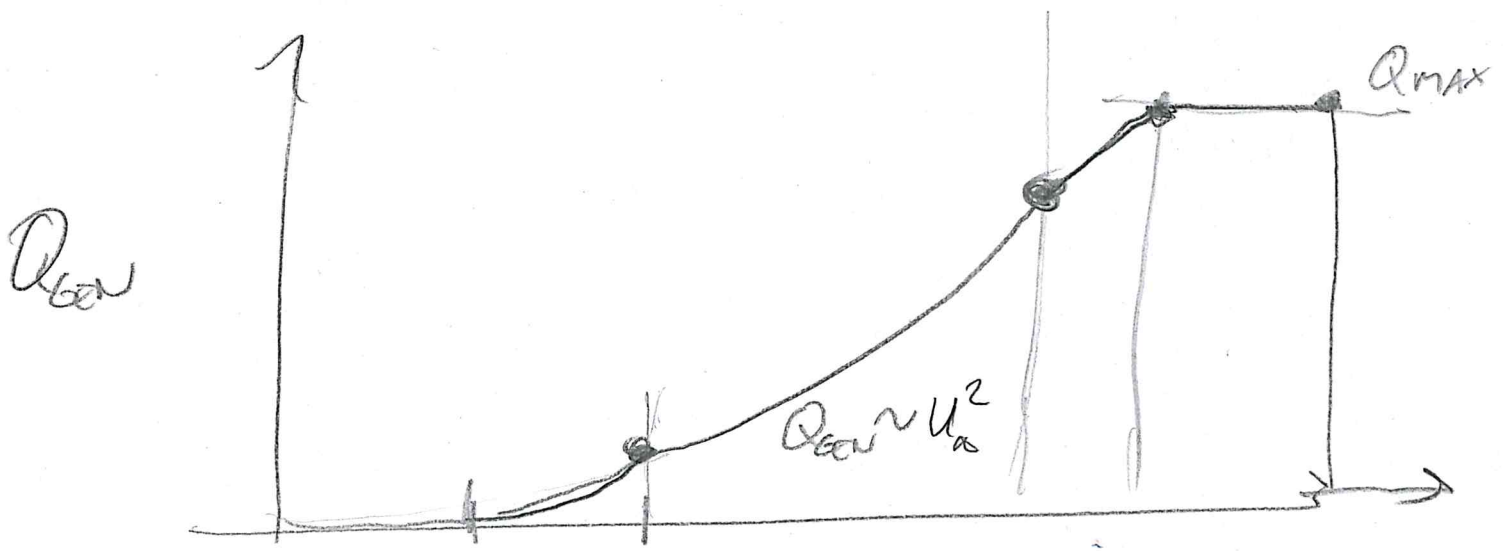
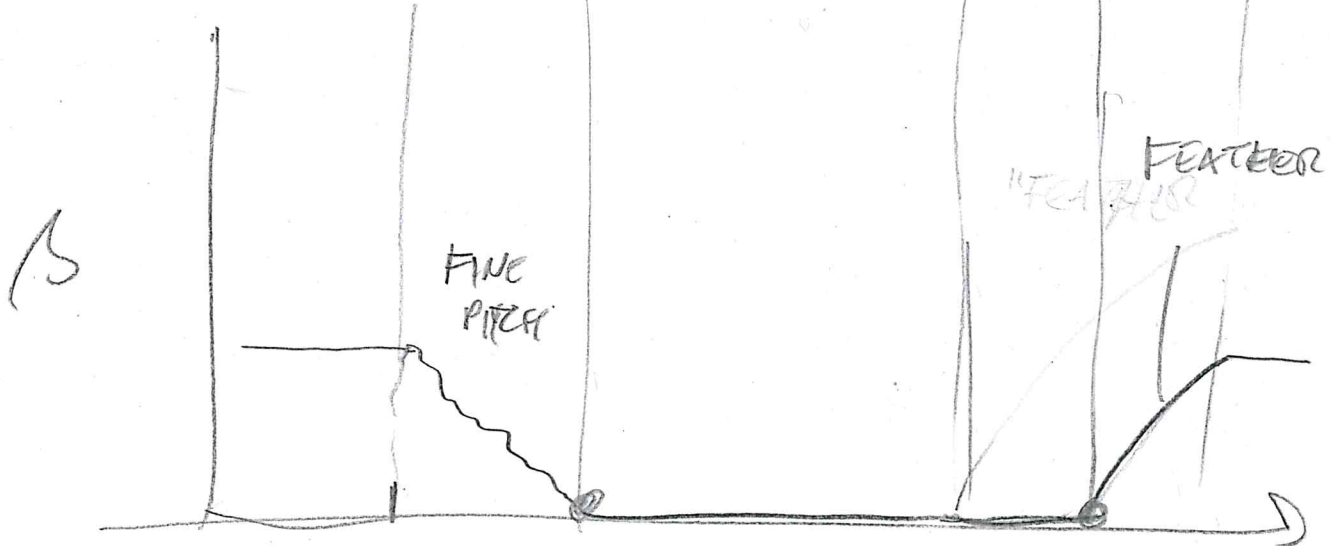
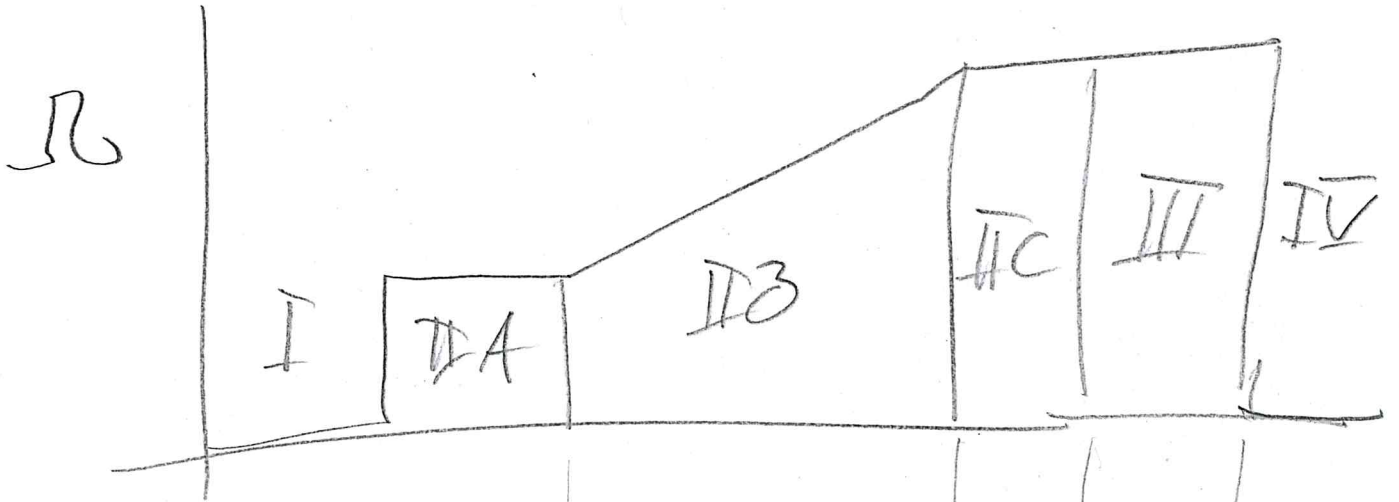
$$\lambda = \frac{R\Omega}{U_{\infty}}$$
 TIP SPEED RATIO

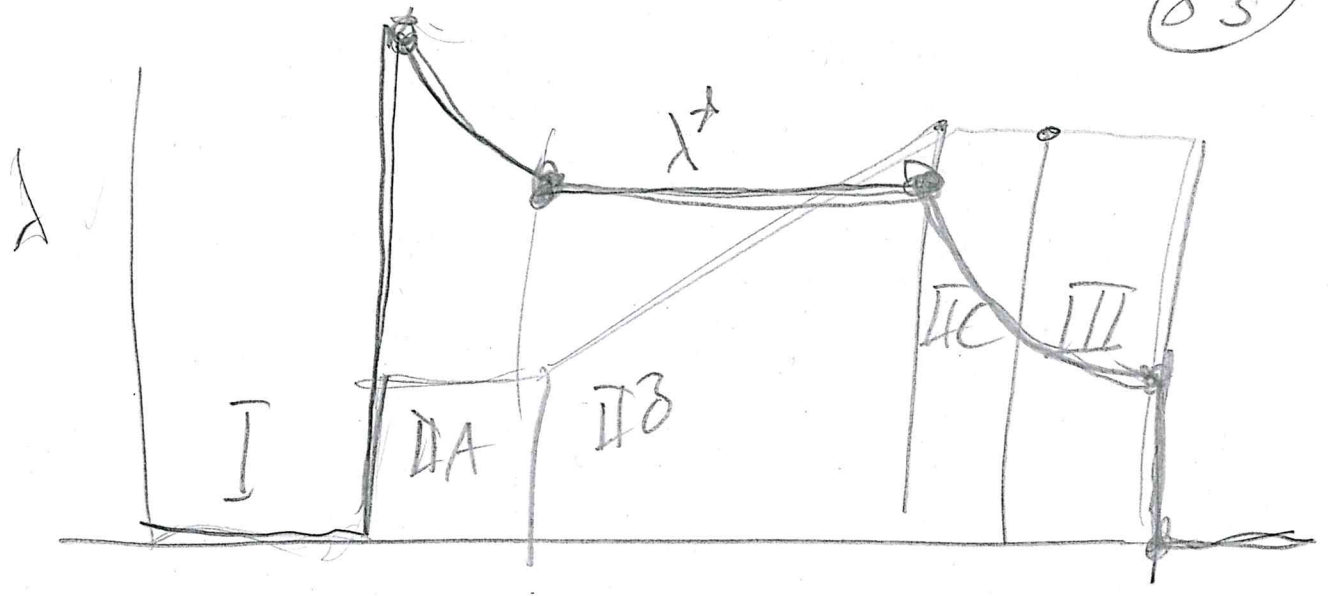
$\beta$  : (COLLECTIVE) BLADE PITCH.

MAXIMUM OF  $C_p$  REACHED FOR  $\lambda^*$  AND  $\beta^*$  (usually 0)  
 $C_{p0} = C_p(\lambda^*, \beta^*)$  (eg. 7)

PITCH & TORQUE VS. WIND SPEED (82)

RECALL:





NOTE: THREE TYPES OF PITCH CONTROL:

- a) COLLECTIVE PITCH (HERE)
- b) CYCLIC PITCH  
(DEPENDING ON AZIMUTH OF BLADE)  
(LIKE HELICOPTERS)
- c) INDIVIDUAL PITCH CONTROL  
(EACH BLADE INDEPENDENTLY CONTROLLED)

IN REGION IIA  $\lambda$  IS FIXED

$\lambda = \lambda_{FIX} = \frac{\Omega_{min} R}{U_{\infty}}$  AND  $\beta$  MAXIMIZES

$C_p(\lambda_{FIX}, \beta)$

IN REGION IIB,  $\lambda = \lambda^*$  AND  $\beta = \beta^*$ ,  
(SUBRATED)

IN REGION III <sup>IIIc &</sup>  $\lambda$  IS AGAIN FIXED TO

$\lambda_{FIX}^{III} = \frac{\Omega_{max} R}{U_{\infty}}$  AND  $\beta$  REGULATES

POWER (III: AT MAXIMUM POWER)

### 5.4 TORQUE CONTROL AT SUBRATED POWER

TORQUE  $Q_{GENERATOR}$  CAN BE CONTROLLED DIRECTLY AND SHOULD COUNTERACT AERODYNAMIC TORQUE  $Q_{AERO}$ . GIVEN ROTOR INERTIA  $I$  WE HAVE ODE FOR  $\Omega$ :

$$I \dot{\Omega} = Q_{AERO} - Q_{GENERATOR}$$

$Q_{AERO}$  DEPENDS ON  $U_{\infty}$  &  $\Omega$  &  $\beta$   
AND IS GIVEN BY

$$P_{AERO} = \Omega \cdot Q_{AERO}, \quad \Omega = \frac{\lambda}{R} \cdot U_{\infty}$$

$$Q_{AERO} = \frac{P_{AERO}}{\Omega} = \frac{1}{2} \rho (\pi R^2) U_{\infty}^3 \frac{C_p(\lambda, \beta) \cdot R}{U_{\infty} \cdot \lambda}$$

$$= \frac{1}{2} \rho \pi R^3 U_{\infty}^2 \left[ \frac{C_p(\lambda, \beta)}{\lambda} \right] =: C_Q(\lambda, \beta)$$

$$= \frac{1}{2} \rho \pi R^3 U_{\infty}^2 \cdot C_Q\left(\frac{\Omega R}{U_{\infty}}, \beta\right) =: Q_{AERO}(\Omega, U_{\infty}, \beta)$$

HOW TO CHOOSE  $Q_{GENERATOR}$ , WHEN ONLY  $\Omega$  IS MEASURED?

IDEA: FIND FUNCTION  $Q_{GENERATOR}(\Omega)$  THAT BRINGS TURBINE TO OPTIMAL TIP SPEED RATIO  $\lambda^*$  (IN REGION II)

INTUITIVELY: • HIGH  $Q_{GEN}$ , IF  $\Omega$  TOO LARGE, (86)

• SMALL  $Q_{GEN}$ , IF  $\Omega$  TOO SMALL

IN ORDER TO STABILIZE ROTOR SPEED.

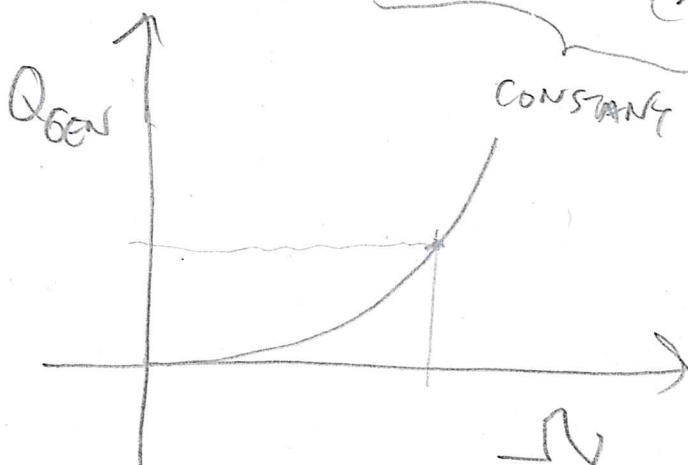
AT OPTIMUM  $\Omega^* = \frac{\lambda^* \cdot U_{\infty}}{R}$  WHERE WE WOULD HAVE

$$Q_{AERO}(\Omega^*, U_{\infty}, \beta^*) = Q_{GEN}(\Omega^*)$$

SO LET US GENERALLY TRY THE LAW

$$\begin{aligned} Q_{GEN}(\Omega) &:= Q_{AERO}\left(\Omega, \frac{R\Omega}{\lambda^*}, \beta^*\right) \\ &= \frac{1}{2} \rho \pi R^3 \left(\frac{R\Omega}{\lambda^*}\right)^2 \frac{C_P(\lambda^*, \beta^*)}{\lambda^*} \end{aligned}$$

$$= \underbrace{\frac{1}{2} \rho \pi R^5 \frac{C_P(\lambda^*, \beta^*)}{(\lambda^*)^3}}_{\text{CONSTANT } K_{GEN}} \cdot \Omega^2$$



(BOSSANYI, 2003)

"MAXIMUM POWER TRACKING TORQUE CONTROL"



IS THIS CONTROL LAW  
STABLE AT  $\Omega^*$  ?

RECALL

Q1)  $\dot{\Omega} = f(\Omega) := \frac{1}{I} (Q_{aero}(\Omega, u_{\infty}, \beta^*) - Q_{gen})$

Q1)  $f(\Omega^*) = 0$ ? (STEADY STATE?)

IF  $\Omega^* = \frac{\lambda^* u_{\infty}}{R}$  THEN BY CONSTRUCTION

$Q_{aero}(\Omega^*, u_{\infty}, \beta^*) = K_{GEN} \cdot (\Omega^*)^2$

SUCH THAT INDEED  $f(\Omega^*) = 0$

Q2)  $\frac{df}{d\Omega}(\Omega^*) < 0$  (STABLE?)

$\frac{df}{d\Omega} = \frac{1}{I} \left( \frac{dQ_{aero}}{d\Omega} - \frac{dQ_{gen}}{d\Omega} \right)$

$= \frac{1}{I} \left( \frac{1}{2} \rho \pi R^3 u_{\infty}^2 \frac{dC_D}{d\lambda} \frac{d\lambda}{d\Omega} - 2 \cdot K_{GEN} \cdot \Omega \right)$

$\frac{dC_D}{d\lambda} = \frac{d\left(\frac{C_p}{\lambda}\right)}{d\lambda} = \frac{\frac{dC_p}{d\lambda} \cdot \lambda - C_p}{\lambda^2} = -\frac{C_p^*}{\lambda^{*2}} \text{ AT } \lambda^*$   
due to optimality

$\frac{d\lambda}{d\Omega} = \frac{R}{u_{\infty}}$

THUS

$$\frac{df}{d\Omega} = \frac{1}{I} \left( \underbrace{\frac{1}{2} \rho \pi R^3 u_{\infty}^2 \left( \frac{C_p^*}{\lambda^{*2}} \right) \frac{R}{u_{\infty}}}_{< 0} - \underbrace{2K_{GEN} \Omega}_{< 0} \right) < 0$$

IN MORE DETAIL, AT  $\Omega = \Omega^* = \frac{\lambda^* u_{\infty}}{R}$   
 WE GET  $u_{\infty} = \frac{\Omega^* R}{\lambda^*}$

$$\frac{df}{d\Omega} = \frac{1}{I} \left( \frac{1}{2} \rho \pi R^5 \right) \left( -\frac{C_p^* \Omega^*}{(\lambda^*)^3} - \frac{2 C_p^* \Omega^*}{(\lambda^*)^3} \right)$$

$$\Rightarrow \frac{1}{2} \rho \pi R^5 \Omega^* \cdot \left\{ C_p^* \right\} \cdot \left\{ \Omega^* \right\}$$

i.e.  $\underbrace{I \cdot (\lambda^*)^3}_{\tau = \text{CONST. [s]}}$   
 SETTLING TIME PROPORTIONAL TO  $\frac{1}{\Omega^*}$  OR  $\frac{R}{u_{\infty}}$

DIMENSIONAL CHECK:

$$I \approx m R^2, \quad m \approx \rho \pi R^3 \Rightarrow I \approx \rho \pi R^5$$

$\rho$ : BLADE DENSITY