# Introduction to TEMPO Summer School on Numerical Optimal Control and Embedded Optimization

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#### Overview

- The University of Freiburg and TEMPO
- Optimal Control Applications and Software
- Overview of the Course
- Introduction of Teachers





## Systems Control and Optimization Laboratory

IMTEK, Faculty of Engineering, University of Freiburg



#### This course's sponsor: the EU Project TEMPO



# Training in Embedded Predictive Control and Optimization

A Marie Curie Initial Training Network (ITN)



14 PhD fellows (all here)

Hosted and trained by TEMPO partner universities and companies:





























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#### Time-Optimal Point-To-Point Motions [PhD Vandenbrouck 2012]





Fast oscillating systems (cranes, plotters, wafer steppers, ...)

#### Control aims:

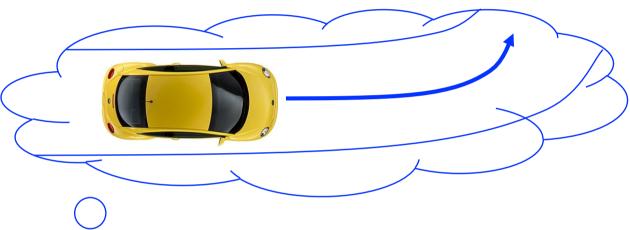
- reach end point as fast as possible
- do not violate constraints
- no residual vibrations

Idea: formulate as embedded optimization problem in form of Model Predictive Control (MPC)



#### Model Predictive Control (MPC)

Always look a bit into the future

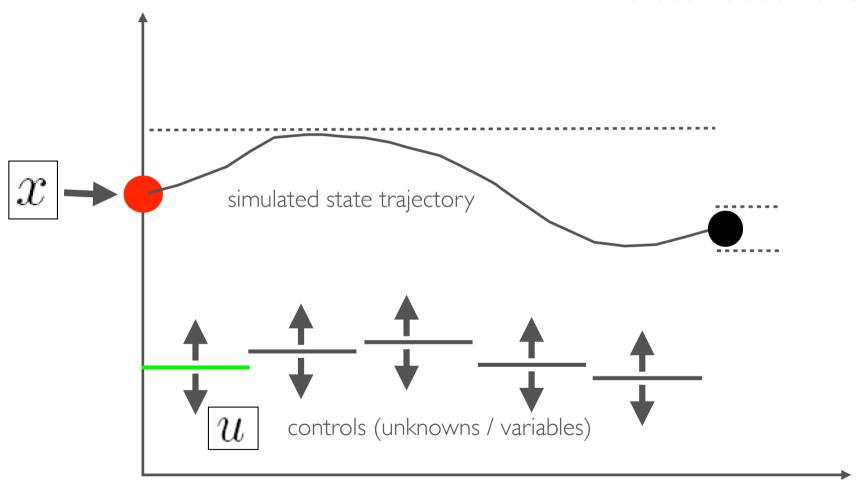




Example: driver predicts and optimizes, and therefore slows down before a curve

#### Optimal Control Problem in MPC

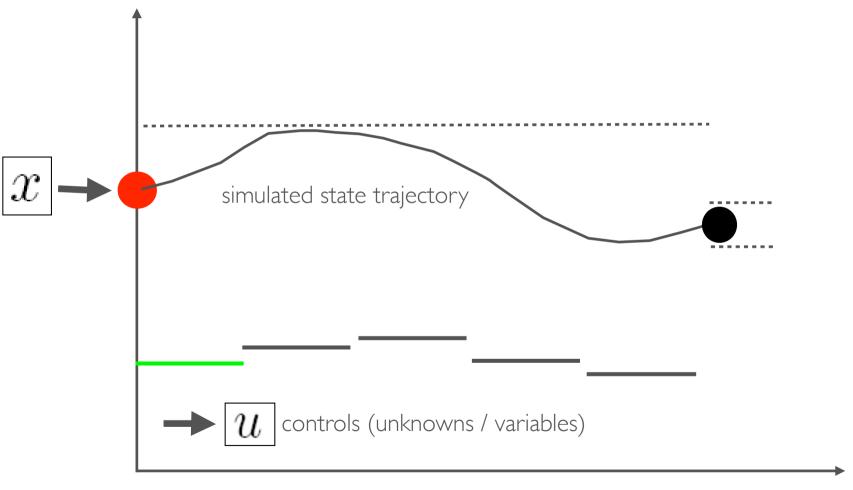
For given system state x, which controls u lead to the best objective value without violation of constraints?



prediction horizon (length also unknown for time optimal MPC)

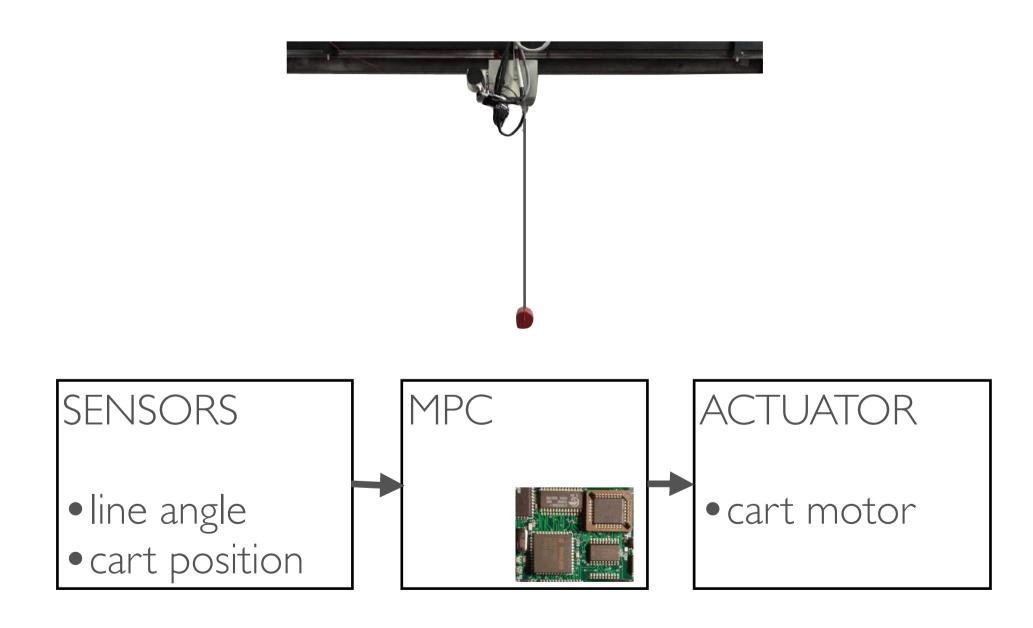
#### Optimal Control Problem in MPC

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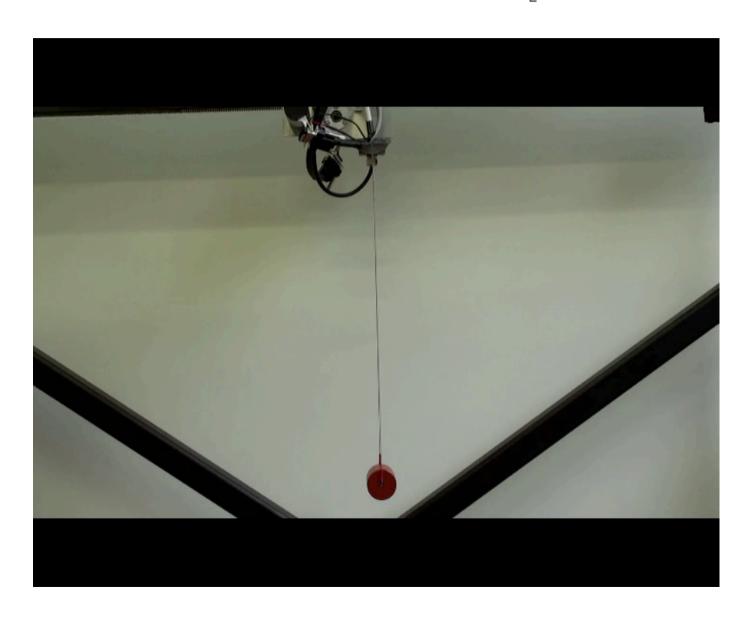
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#### Time Optimal MPC of a Crane

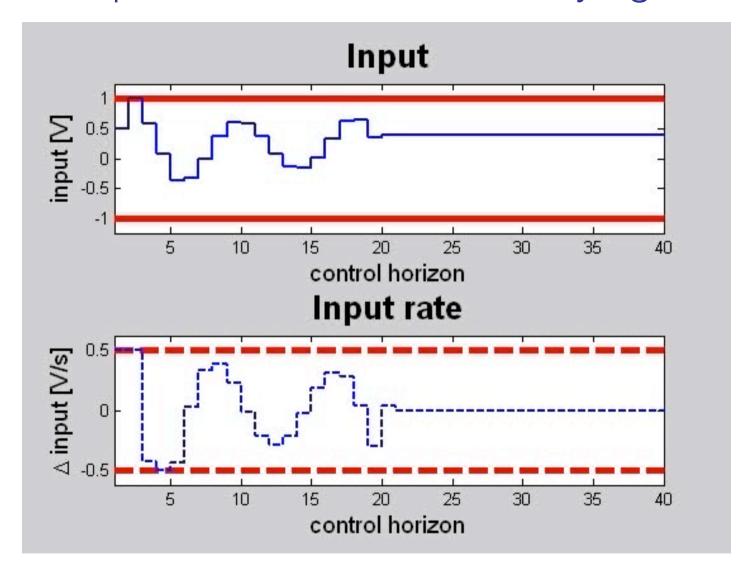


# Time Optimal MPC of a Crane

Univ. Leuven [Vandenbrouck, Swevers, D.]



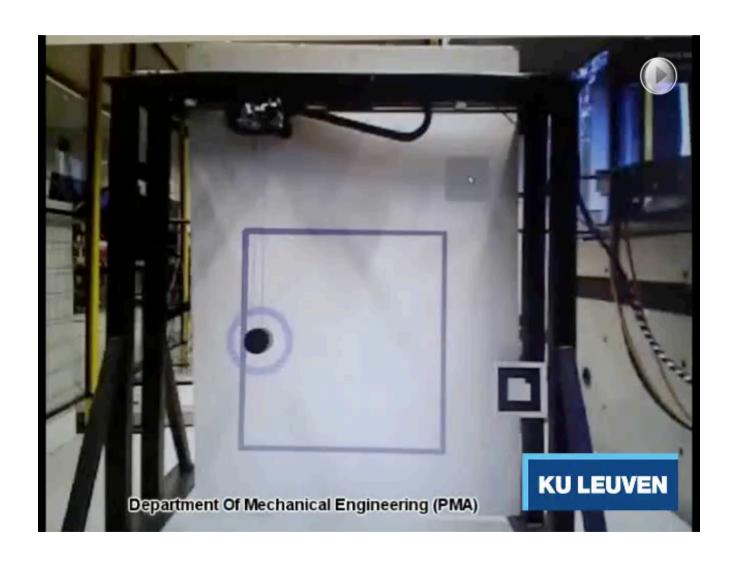
#### Embedded Optimization: Solutions Varying over Time



Solver qpOASES [PhD H.J. Ferreau, 2011], [Ferreau, Kirches, Potschka, Bock, D., A parametric active-set algorithm for quadratic programming, Mathematical Programming Computation, 2014]

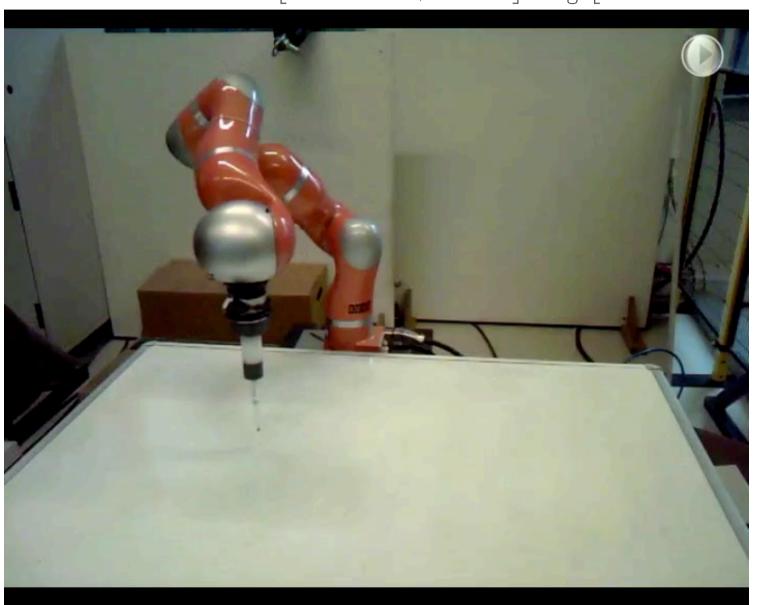
# Time Optimal "drawing" by crane

Univ. Leuven [Wannes Van Loock et al.,] (CasADi)



# Time-optimal "hand writing" by robot

Univ. Leuven [Debrouwere, Swevers] using [Verscheure et al, IEEETAC 2009]



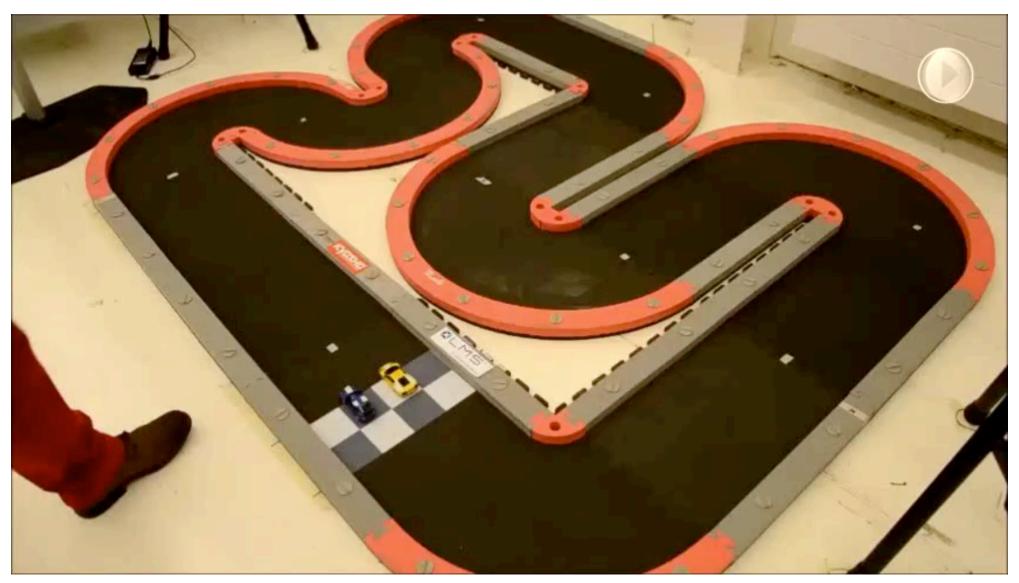
### Robot avoiding a box while moving time optimally

Univ. Leuven [Swevers et al.]



# Time-optimal "racing" of model cars

Univ. Leuven/ETH & LMS [Robin Verscheuren] (ACADO/qpOASES)



#### Software Tools treated in this course

All usable from MATLAB, most open-source

- YALMIP
- qpOASES (LGPL)
- FORCES / FORCES Pro
- ECOS (GPL)
- ACADO (LGPL)
- MPT Toolbox (GPL)
- qpDUNES (LGPL)

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#### **TEMPO Summer School on**

# Numerical Optimal Control and Embedded Optimization

University of Freiburg, July 27 – August 7, 2015

Room 1098, Ground Floor Kollegiengebäude 1 (KG1), Platz der Universität 3, 79098 Freiburg

- two full weeks with lectures, computer exercises, exam, projects, ...
- 60 participants from 13 countries
- 15 organizers and teachers, coordinated by Colin Jones from EPFL (arriving next week), Moritz Diehl and Rien Quirynen

#### First week

	TEMPO Summer School on Numerical Optimal Control and Embedded Optimization, First Week from July 27-31, 2015						
	Monday	Tuesday	Wednesday	Thursday	Friday	Saturday	Su
9:00	Introduction: Systems, Control and Optimization	Nonlinear Simulation and Optimization	Convex Optimization and Sparsity	Alexander Domahidi: Interior Point Methods	Newton Type Optimization		
10:30	Coffee Break	Coffee Break	Coffee Break	Coffee Break	Coffee Break		
11:00	Exercise 1 Linear-Quadratic Regulator	Exercise 3 Newton's Method	Exercise 5 YALMIP	Exercise 7 FORCES	Exercise 9 Gauss-Newton		
12:30	Lunch Break	Lunch Break	Lunch Break	Lunch Break	Lunch Break	Ba	
13:30	Optimal Control Overview	Direct Optimal Control	Joachim Ferreau: qpOASES	Alexander Domahidi: Interior Point Methods	Real-Time Iterations and ACADO	Black Forest Hike	
15:00	Coffee Break	Coffee Break	Coffee Break	Coffee Break	Coffee Break	st H	
15:30	Exercise 2 Dynamic Programming	Exercise 4 Shooting Methods	Exercise 6 qpOASES for MPC	Exercise 8 ECOS	Exercise 10 ACADO Code Generation	ike	
17:00	Break	Break	Break	Break	Break		
17:20	Review Session	Review Session	Review Session	Review Session	Review Session		
18:00	End	End	End	End	End		
	18:30 Reception**		18:00 Guided City Tour	18:30 Dinner Reservation (self-payment)*			

#### Second week

TEMPO Summer School on Numerical Optimal Control and Embedded Optimization, Second Week from August 3-7, 2015								
	Monday	Tuesday	Wednesday	Thursday	Friday			
9:00	Exam	Alternating Direction Method of Multipliers	Block Condensing for qpDUNES	Project Work	Project Presentations			
10:30	Coffee Break	Coffee Break	Coffee Break	Coffee Break	Coffee Break			
11:00	Explicit MPC	Exercise 12 ADMM	Project Work	Project Work	Project Presentations			
12:30	Lunch Break	Lunch Break	Lunch Break	Lunch Break	Project Presentations			
13:30	Explicit MPC	Project Work	Project Work	Project Work	End			
15:00	Coffee Break	Coffee Break	Coffee Break	Coffee Break				
15:30	Exercise 11 Explicit MPC	Project Work	H. G. Bock Efficient Methods for Inverse Optimal Control Problems	Project Work				
17:00	Break	Break	Break	Break				
17:20	Review Session and Project Commitments	Systems Control and Optimization Lab Tour	Project Work	Project Work				
18:00	End	End	End	End				

18:30 Dinner\*\*

#### List of Organizers and Teachers

Name	Institution		
Prof. Dr. Dr. h.c. mult. Hans Georg Bock	Heidelberg University, Germany		
Prof. Dr. Moritz Diehl	University of Freiburg, Germany		
Dr. Alexander Domahidi	Embotech, Switzerland		
Dr. Joachim Ferreau	ABB, Switzerland		
Jean Hours	EPFL, Switzerland		
Prof. Dr. Colin Jones	EPFL, Switzerland		
Milan Korda	EPFL, Switzerland		
Dimitris Kouzoupis	University of Freiburg, Germany		
Dr. Michal Kvasnica	Slovak University, Slovakia		
Adeleh Mohammadi	KU Leuven, Belgium		
Christine Paasch	University of Freiburg, Germany		
Rien Quirynen	University of Freiburg, Germany		
Georgios Stathopoulos	EPFL, Switzerland		
Pu Ye	EPFL, Switzerland		
Mario Zanon	University of Freiburg, Germany		